

μ SR study of the quantum dynamics in the frustrated $S = \frac{3}{2}$ kagomé bilayers

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We present μ SR experiments in the $S = \frac{3}{2}$ kagomé bilayer compound $\text{Ba}_2\text{Sn}_2\text{ZnGa}_{10-7p}\text{Cr}_7p\text{O}_{22}$ (BSZCGO(p)) and compare it to the isostructural $\text{SrCr}_9p\text{Ga}_{12-9p}\text{O}_{19}$ (SCGO(p)), including for the latter new results for $p \geq 0.89$. Quantum-dynamical low energy magnetic excitations are evidenced in this novel compound. We study the evolution of the muon relaxation rate with p , T and field. A phenomenological model for the muon relaxation based on sporadic dynamics due to spin excitations in a singlet sea proposed by Uemura *et al.* [Phys. Rev. Lett. **73**, 3306 (1994)]. is extended to all fields and T -range. Its connexion to the RVB picture is discussed, and we argue that such coherent states might mediate the interactions between “impurities” which induce the spin glass freezing.

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The stabilization of a spin liquid state, in which all kinds of magnetic correlation functions are short ranged, seems now granted theoretically in the $S = \frac{1}{2}$ Heisenberg kagomé lattice with nearest neighbour (NN) antiferromagnetic interactions. The ground state (GS) is probably of resonating valence bond type (RVB), built from a macroscopic number of singlet states [1]. If any, a gap between the GS and the first triplet state is expected to be fairly small ($\sim J/20$) [2] in comparison with the exchange constant J . Most striking, due to both corner sharing geometry and half integer spins, an exponential density of low lying singlet excitations, with energies smaller than the gap, is predicted [3] and yields an extensive entropy at $T = 0$ [4]. Finally, the nature of the first magnetic excitations, such as unconfined spinons, are still under debate [4].

Among all corner sharing highly frustrated magnets, only a few are good candidates fulfilling the important conditions of the pure Heisenberg lattice with NN couplings. The combination of the weakness of the single-ion anisotropy and of a direct overlap exchange are certainly the major advantages of the recently discovered chromate $S = \frac{3}{2}$ kagomé bilayer BSZCGO(p) [5, 6] and the long studied SCGO(p) [7], where p is the Cr^{3+} network covering rate. Beyond the absence of ordering well below the Curie-Weiss temperature, the unusual large value of the specific heat unveils a high density of low lying excitations [5, 8] and its field independence suggests that the excited states are mostly singlets [9]. Moreover, their GS is found essentially fluctuating as proven by neutron experiments [10], and μ SR for SCGO(p) [11, 12], although an intrinsic spin glass (SG) signature is observed in susceptibility measurements [7, 13]. The origin of such a SG state in a disorder-free system still awaits for a complete understanding although recent theoretical approaches catch some of the facets of this original GS [14].

In this context BSZCGO(p) appears as a unique com-

pound : it has a more pronounced 2D character than SCGO(p), with a larger interbilayer distance [5] and *all* the magnetic sites lying on a corner sharing lattice [22]. In addition, a twice lower SG temperature T_g has been reported [5] and a new type of defects other than non-magnetic substitutions (likely bond defects), dominates the low- T susceptibility [6]. This offers the possibility of probing the influence of T_g and the relevance of dilution on the evolution of the $T \rightarrow 0$ dynamics, by a simple comparison of two quasi-identical kagomé bilayers.

In this Letter, we present the first Muon Spin Relaxation (μ SR) study of the spin dynamics in BSZCGO(p) and revisit the case of SCGO(p) for low dilutions now available. This technique has proven to be a front tool for the study of quantum dynamical states in a vast family of singlet GS systems. Whereas specific heat is sensitive to all kinds of excitations, including likely dominant low lying singlets at low- T [9], muons (μ^+ , $S = \frac{1}{2}$) probe *magnetic excitations only*. Their relaxation rate λ is linked to the spin-spin time correlation function $\lambda = 1/T_1 \sim \int_0^\infty \langle \mathbf{S}(0) \cdot \mathbf{S}(t) \rangle \cos(\gamma_\mu H_{LF} t) dt$, where H_{LF} is the external field applied along the μ^+ initial polarization and γ_μ is the μ^+ gyromagnetic ratio. The typical time window (10 ns-10 μ s) allows to observe spin fluctuations which set in the specific range of frequencies ($\sim 10^9$ Hz) in between NMR and neutron experiments. Not only in SCGO [11, 12] and in other kagomé systems [15, 16] but also in other spin-singlet compounds [17], the signature of the quantum dynamics when $T \rightarrow 0$ could be identified to the occurrence of a plateau of λ and a field-independent initial Gaussian shape of the μ^+ polarisation $P_z(t)$. Extending the original guess of Uemura *et al.* to explain this exotic fluctuating GS [11], we propose for the first time a phenomenological model which explains both T - and field-dependence of $P_z(t)$ for all p in these kagomé bilayers.

In order to illustrate the evolution of the properties

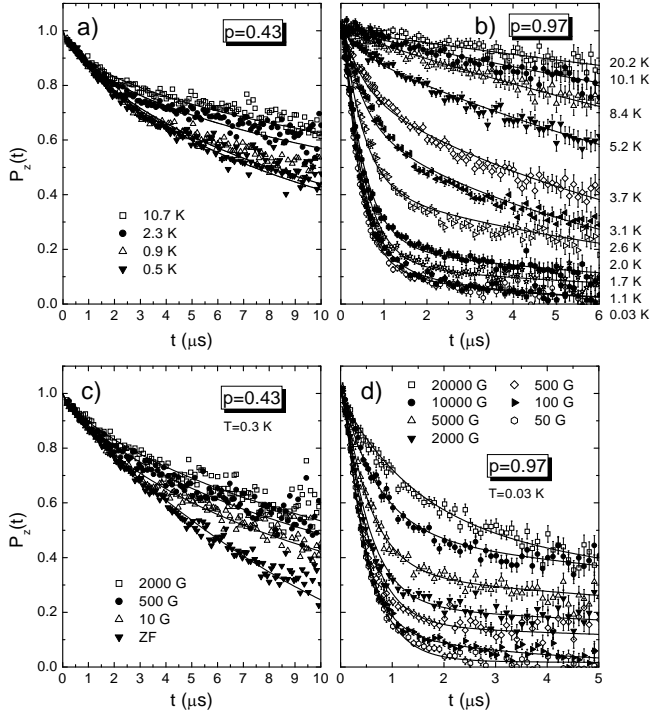


FIG. 1: a,b) T -dependence of the μ^+ polarization $P_z(t)$ in BSZCGO under weak (10 G for $p = 0.43$ and 100 G for $p = 0.97$) longitudinal field. Notice the different time scales for both samples. c,d) H_{LF} -dependence at base- T . The line for $p = 0.43$, ZF, is a square-root exponential multiplied by the Kubo-Toyabe function in zero field ($\Delta_{ND} \sim 0.08 \mu s^{-1}$), to take into account the nuclear dipole contribution. The other lines are fits described in the text.

with dilution, we first focus on the qualitative differences (Fig. 1) between two typical low and high occupations p of the kagomé bilayers. Starting from high- T ($T > 6$ K in Fig. 1(a,b)), a conventional paramagnetic behavior is found for both cases, with an exponential variation of $P_z(t)$ in the dense case and square root exponential in the dilute case. The evolution of $P_z(t)$ at low- T is markedly different. For $p = 0.97$, the relaxation rate increases by more than two orders of magnitude to reach a T -independent value for $T \lesssim T_g \approx 1.5$ K [5] (Fig. 1(b)). For $T = 0.03$ K, $P_z(t)$ displays a shape in between exponential and Gaussian at early times and reaches zero value at long times (Fig. 1(d)). It also displays a much weaker field dependence than for a frozen magnetic state. Indeed, for $\lambda \sim 2 \mu s^{-1}$, a 500 G field would completely decouple the μ^+ polarisation [11]. Following the arguments initially developed for SCGO(p) [11, 12], all these properties are the first indications of a quantum dynamical magnetic state in BSZCGO(0.97). For $p = 0.43$, we also find a dynamical state but, at variance with the previous case, only a weak T -dependence is observed. Also, the polarization displays a square root exponential decay for all T (Fig. 1(a)) and for any field H_{LF} (Fig. 1(c)). A

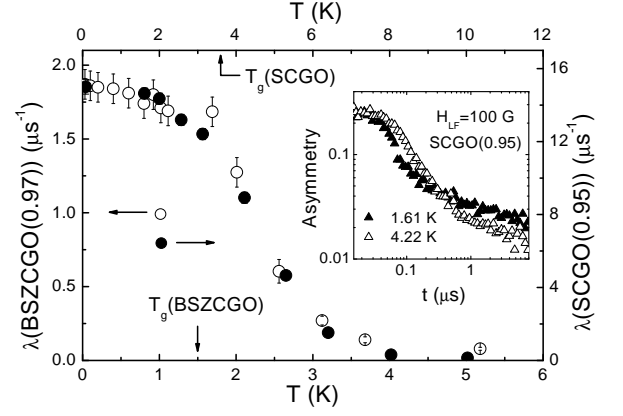


FIG. 2: Comparison of the evolution of the μ^+ relaxation rate λ vs. T in BSZCGO(0.97) and SCGO(0.95), from a $1/e$ analysis. Inset : recovery of a part of the asymmetry at low- T and long times in SCGO below T_g (log-log scale).

weak plateau of the relaxation rate is still observed below 0.5 K. However the relaxation rate increases weakly but continuously when T decreases for $p = 0.3$, with a very weak H_{LF} -dependence. This is typical of the pure paramagnetic fast fluctuations limit for diluted magnetic systems, although strongly frustrated antiferromagnetic interactions are still reported [6].

In a first step of analysis, we estimate the μ^+ relaxation rate λ using the $\frac{1}{e}$ point of $P_z(t)$, as discussed in [12]. This allows to single out information about two important issues using a simple model-independent analysis : the role of the SG-like transition and the impact of the non-magnetic dilutions on the dynamics.

From high- T , λ increases by more than two orders of magnitude down to T_g for both purest samples, to reach the relaxation rate plateau $\lambda_{T \rightarrow 0}$ for $T \lesssim T_g$. With a T -scale twice larger for SCGO(0.95) than in BSZCGO(0.97), $\lambda(T)$ perfectly scales on the T axis as shown in Fig. 2 [23]. This ratio is very close to their T_g ratio of 2.3(2), which points to a link between the formation of the SG-like state and the presence of quantum fluctuations. This seems to be a quite common feature of various systems with singlet GS systems [11, 12, 15, 16, 17].

In Fig. 3 we report the variation of $\lambda_{T \rightarrow 0}(T)$ for various BSZCGO(p) samples and compare them to SCGO(p) [11, 12]. Although additional p -independent defects are dominant in BSZCGO(p) and evidenced from a large Curie-like term in macroscopic susceptibility at low- T [6], it is very surprising to find a very similar quantitative $\lambda_{T \rightarrow 0}$ variation in the *whole* p range for both systems. Therefore we conclude that *only* defects related to *dilution* influence the relaxation rate.

In a classical framework, a coplanar arrangement with zero-energy excitation modes, involving spins on hexagons, was proposed in the literature to be selected at low- T [18]. Inelastic neutron scattering experiments on

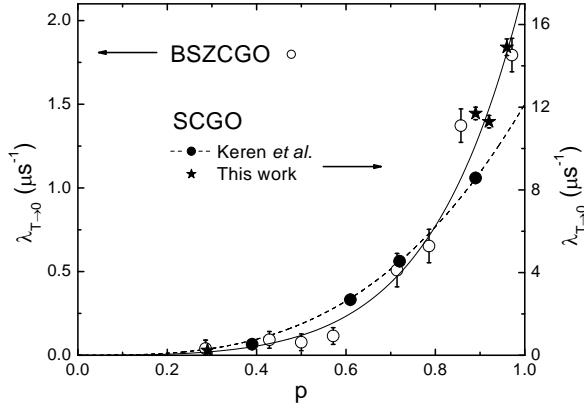


FIG. 3: p -dependence of $\lambda_{T \rightarrow 0}$ for BSZCGO (open symbols) and SCGO (full symbols). Continuous (dashed) lines are $\sim p^3 + 1.9(3)p^6$ ($\propto p^3$, [12]) fits.

the spinel compound ZnCr_2O_4 are the first recent indication in favor of such excitations [19]. Therefore, one expects the μ^+ relaxation to scale with the number of fully occupied hexagons, $\propto p^6$. The BSZCGO(p) data altogether with our SCGO $0.89 \leq p \leq 0.95$ samples indicate that $\lambda_{T \rightarrow 0}(p)$ is well accounted for by adding a dominant p^6 term to the $\propto p^3$ term proposed for SCGO($p \leq 0.89$) in [12] (Fig. 3). This certainly indicates that the relaxation is not induced by single spin excitations but rather *collective* excitation processes extending at least on triangles and hexagons.

One of the pending challenges in the analysis of μSR in kagomé frustrated antiferromagnets is to find a theoretical model reproducing $P_z(t)$ for *all* fields and *all* temperatures. In the quantum framework of a singlet GS, one needs unpaired spins in order to generate magnetic excitations responsible for the μ^+ relaxation. Such excitations can be ascribed by spin $\frac{1}{2}$ unconfined spinons. Their location vary in time with no loss of coherence of the excited state. Hence, a given μ^+ couples to a spin only a short fraction ft of the time t after implantation and one can use a model of “sporadic” field fluctuations to describe $P_z(t)$. This was the initial guess by Uemura *et al.* to account for the weakness of the field dependence of $P_z(t)$ at low- T in SCGO(0.89) [11]. This polarization is given by a “sporadic” dynamical Kubo-Toyabe function which can be approximated by the Keren analytical function $P_z^K(ft, \Delta, H_{LF}, \nu) = P_z^K(t, f\Delta, fH_{LF}, f\nu)$, valid in the limit $\nu \geq \Delta$ [20], quite appropriate here. Δ/γ_μ is the local field created on the μ^+ site by a paramagnetic neighbouring released spin, with a corresponding exponential time correlation function, $\exp(-\nu t)$, characterized by a fluctuation frequency ν . Δ is related to the μ^+ location in the unit cell and its value is therefore p -independent for a given system but is expected to vary from BSZCGO to SCGO. The Gaussian at early times, the weakness of the field dependence and a dynamical relaxation down to

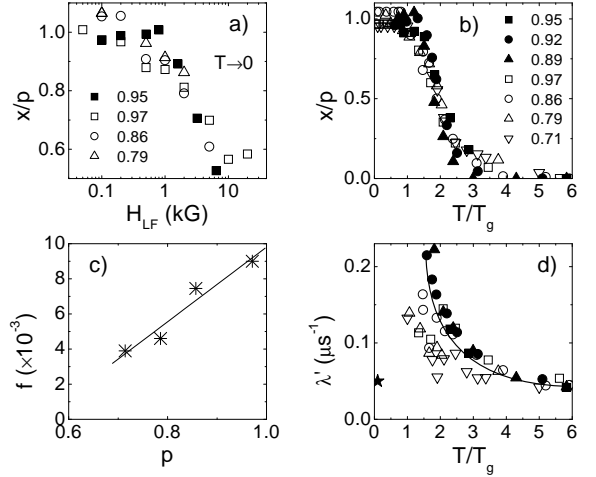


FIG. 4: Fitting parameters of Eq. 1. a,b) H_{LF} - and T -dependence of x for BSZCGO(p) (open symbols) and SCGO(p) (full symbols). c) p -dependence of f . d) T -dependence of λ' .

0 are altogether related to the f factor and $\nu \sim \Delta$. In addition to this sporadic relaxation, we found that a more conventional Markovian relaxation channel needs to be introduced in order to fit the long times tail ($t \gtrsim 3 \mu\text{s}$) for all fields and T , which yields an exponential variation of $P_z(t)$. We therefore write

$$P_z(t) = xP_z^K(t, f\Delta, fH_{LF}, f\nu) + (1-x)e^{-\lambda't}, \quad (1)$$

where x represents the weight of the short time sporadic dynamical function, associated with the spinons dynamics. In the following, we first detail how all these parameters can be reliably deduced from the data and sketch a physical picture consistent with our results.

We first present our analysis for $T \ll T_g$ in BSZCGO(p). In order to limit the number of free parameters, we make the minimal assumption that the external field does not influence the dynamics of the coherent spinon term. ν and Δ values are shared for all p and H_{LF} and are set by our data taken at low fields ($H_{LF} < 500$ G) for various p . f is adjusted for each p and its variation accounts for the evolution of $\lambda_{T \rightarrow 0}(p)$. For low fields, x is found close to 1 for the purest samples (Fig. 1(a,b)), making λ' a non-relevant fitting parameter. On the contrary, the high field data enable us to track the evolution of x with H_{LF} and to determine a value of λ' . We could not extend the fits below $p = 0.71$ since the weak field dependence prevents an unambiguous determination of the parameters.

We find perfect fits of our data (Fig. 1(d)) with $\nu \sim 1000 \mu\text{s}^{-1}$, $\Delta \sim 350 \mu\text{s}^{-1} \sim \gamma_\mu \times 4$ kG and an average value of $f \sim 0.006$. We find a nearly flat p -independent long time relaxation rate for $T \ll T_g$ ($\lambda' \sim 0.05 \mu\text{s}^{-1}$, ★ in Fig. 4(d)). An important finding is that x is of the order of p at low fields (Fig. 4(a,b)). This may be re-

lated to theoretical computations showing that the correlations are enhanced around spin vacancies in the kagomé lattice [21], which would destroy locally the liquid state. Besides, x decreases appreciably for $H_{LF} \sim 10$ kG whatever the value of p . We can associate this decrease to the existence of an energy scale ~ 1 K, which is of the order of T_g . Finally, we observe a linear variation of f with p (Fig. 4(c)) and f tends to vanish around $p \sim 0.5$, a limit consistent with our classical approach (Fig. 3). This indicates that even far from the substituted sites, the coherent state is somehow affected, e.g the density of spinons could be smaller.

As suggested by the similar p -variation of $\lambda_{T \rightarrow 0}$ in both BSZCGO and SCGO, we assume that the excitation modes are identical in both systems, i.e., f and ν are kept the same for comparable p . We find $\Delta \sim 1200 \mu\text{s}^{-1}$ for our SCGO samples ($p \geq 0.89$), in agreement with previous work on SCGO(0.89) [11]. In order to cross-check these values of Δ , we use the high- T (~ 50 K) data for BSZCGO (SCGO), $\lambda \sim 0.01 \mu\text{s}^{-1}$ ($0.03 \mu\text{s}^{-1}$). In the appropriate paramagnetic limit, the fluctuation rate can be estimated from $\nu \sim \sqrt{z}JS/k_B\hbar \sim 2 \times 10^{13} \text{s}^{-1}$ [11] using a coupling $J = 40$ K [6] and an average number $z = 5.14$ of Cr NN [7]. We extract $\Delta = \sqrt{\lambda\nu/2} \sim 300 \mu\text{s}^{-1}$ ($600 \mu\text{s}^{-1}$), consistent with our fits. It is quite rewarding to find that a *common* physical picture underlies all the sets of data at low- T for *both* kagomé bilayers.

We now extend the fits of $P_z(t)$ to the whole T -range (Fig. 1(b)), fixing f to its low- T value in order to limit the number of free parameters. As expected from the change of shape around T_g [11, 12], the weight x of the sporadic term decreases to finally enter a high- T regime (Fig. 4(b)) where the μ^+ relaxation becomes exponential ($x \rightarrow 0$). Notice the similarity between the field and T -dependence of x which indicates that the sporadic regime is destroyed when the energy is of the order of T_g . Fig. 3(b) displays a sharp crossover from one state to the other, between T_g and $\sim 3T_g$, corresponding to the λ steep decrease (Fig. 2), for both BSZCGO(p) and SCGO(p). For $T > T_g$, ν and λ' (Fig. 4(d)) decrease by one order of magnitude up to $\sim 10T_g$.

At high- T , it is natural to think in terms of paramagnetic fluctuating spins. Lowering T , λ' seems to diverge at T_g and below, the weight of the exponential term at low fields ($1 - x \sim 1 - p$) could correspond to localized frozen spins, reflecting a glassy component. It is noteworthy that T_g does not increase with $1 - p$ but rather decreases, at the opposite of the case of canonical spin glasses. We could further confirm the existence of such a frozen component in SCGO($p = 0.95 - 0.89$), since a clear recovery of a small part ($\sim 4\%$) of the asymmetry is found at long times (e.g. Fig. 2(inset)). It is observed for $t \sim 100 \lambda^{-1}$, which is out of the experimental range in the case of BSZCGO(p).

To summarize, the picture based on a coherent RVB state, which magnetic excitations are mobile fluctuating

spins $\frac{1}{2}$ on the kagomé lattice, explains well the data, provided that (i) these excitations can be generated even for $T \rightarrow 0$. This underlines the smallness of the “magnetic” gap, if any, typically $\Delta < J/1000$; (ii) an energy scale related to T_g (fields of the order of 10 kG or, equivalently, temperatures of the order of T_g , which vary very little with p) are high enough to destroy the coherent RVB type state; (iii) the substitution defects are accounted for by an additional classical relaxation process.

The absence of energy scale for spin $\frac{1}{2}$ excitations could explain quite well why the transition to the SG state is fairly independent of p . Indeed, in this framework, spinons could mediate the interactions between magnetic defects localized around spin vacancies. This is corroborated by all the scaling properties in T/T_g . The transition to the SG state corresponds then to the formation of the coherent singlet state rather than any interaction strength between defects.

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- [22] On the contrary, SCGO(p) has Cr pairs in between the bilayers.
- [23] We attribute the factor 8 between λ in both systems to a different coupling of the μ^+ to the Cr spins. Transverse

field experiments show for instance a larger linewidth in SCGO(0.95) than in BSZCGO(0.91) (D. Bono *et al.*, *unpublished*) despite a lower defect term [6].